Programming with nominal techniques

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Thanks

Thank you to the organisers Yukiyoshi Kameyama, Ohad Kammar, and Jeremy Yallop for organising this school, for allowing me to participate – and for asking me to give this talk.

Advert: Nominal Techniques Summer School

3rd School on Foundations of Programming and Software Systems

(FoPSS 2019, co-located with HIGHLIGHTS 2019) Warsaw, 10–15 September 2019

https://www.mimuw.edu.pl/~fopss19/

Johannes Borgström Bartek Klin Jamie Gabbay Andrew Pitts Maribel Fernández Mikołaj Bojańczyk Sławomir Lasota Andrzej Murawski Nominal Process Calculi and Modal Logics Basic Nominal Techniques Advanced Nominal Techniques Nominal Sets and Functional Programming Nominal Rewriting and Unification Computation Theory with Atoms Computation Theory with Atoms II Nominal Game Semantics

Nominal techniques ...

... are an approach to **names** and **name-binding/abstraction** based on semantics in sets with atoms and Choice (ZFAC) [gabbay:equzfn].

Examples of names in TCS include:

- Variable symbols: the 'x' in $\lambda x.x$.
- Pointers / (pointer = name + deref).
- Variables x (variable = name + substitution).
- Channel names a (cf. π -calculus).
- Thread IDs, file handles, & similar.
- Meta-variables (= name + capturing substitution).
- ▶ Wires in diagrams (cf. Ghica).
- Orbit-finite sets.
- ...and more.

Nominal techniques ...

... are an approach to names and name-binding/abstraction based on semantics in **sets with atoms and Choice** [gabbay:equzfn] (ZFAC set theory).

The theory is foundational. Thus, it lends itself to an account of what names *are* — may be distinct from account of how names are *programmed on*, or even account of how a *particular kind* of names is programmed on.

Analogy: arguably numbers *are* the smallest set closed under 0 and succ — yet implementations use e.g. binary strings.

The implementation may only approximate the mathematical model:

- E.g. numbers are unbounded but int64 is bounded.
- Floating point arithmetic may be imprecise, even for whole numbers.
- Division is a partial function (divide-by-zero), but be approximated by a total type like Int × Int → Int, → ≥ → ∞ ~ 5/30

There may even be multiple implementations of the same model, just as \mathbb{N} underlines multiple numeric datatypes. Even lists have this: e.g. mapped-to-memory vs. linked lists.

Possible for nominal techniques to exist in theory & user model — yet datatypes implemented e.g. using de Bruijn indexes.

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Other name-carrying structures, such as orbit-finite sets, might require other concrete implementation.

A wee, provocative tangent

Misunderstandings arise when people fail to distinguish between mathematical models and their implementations (if any).

- There are people who literally know that binding = λ-abstraction, and
- other people who know that binding = numbers & de Bruijn, and
- other people who know that binding doesn't exist at all ... it's all combinators!

I suspect the maths is more real than the implementation.

How else do you explain that there are people who *know* that programming = Java, or programming = Python, or that effects don't exist (all programming is pure), or that *only* effects exist (pure programs are just sugar)?

Here, maths, especially logic, (helps to) teach tolerance.

Nominal techniques

I won't describe the mathematical nominal sets model of names and binding in this talk. That's for another lecture series. (Go to the nominal summer school advertised above if you like!)

Here, I want to focus on implementation.

Previous efforts, such as in my PhD thesis, FreshML, and FreshOCaml, have either tried to

- extend a language systematically with nominal constructs (thus generating a dialect), or
- to deeply embed names and permutations inside an existing language (thus costing the polymorphic advantage of the nominal style).

I want to talk about how to host nominal techniques polymorphically inside a language, as a guest, i.e. as a package, in a new way.

Key feature of nominal techniques

The nominal model of names is polymorphic over types.

I will sketch a package which provides constructs which

- may be weaker than full nominal techniques, and may be unsafe (i.e. raise runtime errors if abused) but
- can be 'just loaded' and
- are type polymorphic.

Unclear how to do this. I will first:

propose solution (high-level, language-independent), then

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suggest implementations.

Your challenge:

Make it real; implement it.

My proposal follows:

Type-formers

Name : $* \rightarrow *$ Nom : $* \rightarrow * \rightarrow *$

• a : Name au says

a is a name. a carries a label of type τ (like ' τ -ref').

x : Nom τ α says
 x is an element in α.
 Some τ-labelled names may be abstracted in x.

(Or Nominal : $* \rightarrow *$ where x : Nominal α means x is an element in α with names of possibly many different types abstracted; stick to one τ for concreteness.)

 $\tau\text{-labels}$ as object-level typing info

 τ -labels are optional, but convenient. Write () for the unique element of the unit type. Then:

a : Name() says

 I am a name.
 I have a label, but it's trivial so call me a pure name.

 x : Nom()(Name()) says

I am a pure name. I may be bound.

 τ -labels are convenient because many TCS applications involve type environments, as in 'a : N' — intuitively, N : τ and (a : N) \in Name τ . So: τ -labels save us threading an environment of type annotations.

Constructors and destructors

Name : $* \to *$ Nom : $* \to * \to *$ fresh : $\forall \tau. \tau \to \operatorname{Nom} \tau$ (Name τ) res : $\forall \tau, \alpha$. [Name τ] $\times \alpha \to \operatorname{Nom} \tau \alpha$ label : $\forall \tau, \alpha$. Name $\tau \to \tau$

[...] denotes lists.

- fresh(t) generates a fresh t-labelled name n and wraps it in an n-binding.
- res(*l*, *a*) (where res = 'restrict') inputs a list of names *l* and *a* : α, and wraps *a* in an *l*-binding.
- label(n) returns whatever value n points at.

Constructors and destructors

Name : $* \to *$ Nom : $* \to * \to *$ fresh : $\forall \tau. \tau \to \operatorname{Nom} \tau$ (Name τ) res : $\forall \tau, \alpha$. [Name τ] $\times \alpha \to \operatorname{Nom} \tau \alpha$ label : $\forall \tau$. Name $\tau \to \tau$

res is associative, the order of the elements in *I* doesn't matter, and we have weakening. The list is just a convenience.

res is dynamic, or capturing. E.g.

 $(\lambda a.res([n], x)) n \rightarrow res([n], n).$

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Nom is a monad

Omit top-level type quantifiers henceforth.

Name : $* \rightarrow *$ Nom : $* \rightarrow * \rightarrow *$ fresh : $\tau \rightarrow \operatorname{Nom} \tau$ (Name τ) res : $[Name \tau] \times \alpha \rightarrow Nom \tau \alpha$ label : Name $\tau \rightarrow \tau$ return : $\alpha \rightarrow \operatorname{Nom} \tau \alpha$ >>=: Nom $\tau \alpha \rightarrow (\alpha \rightarrow \text{Nom } \tau \beta) \rightarrow \text{Nom } \tau \beta$

- \blacktriangleright Nom τ is a monad, for each τ .
- return = λa .res([], a) wraps $a : \alpha$ in an empty binding context.

>>= is capture-avoiding. E.g. monadic combination of res([n], n) with res([n], n) is $res([n_1, n_2], (n_1, n_2))$. See 'Nom equality' slide below. Unsafe operations on Nom (probably private)

unNom : Nom $\tau \alpha \rightarrow \alpha$ fuse : Name $\tau \rightarrow$ Name $\tau \rightarrow$ Nom τ ()

unNom destroys binding. Unsafe because names can escape scope:

unNom res $(n, a) \rightarrow a$ so that unNom (fresh ()) \rightarrow unNom (res([n], n)) $\rightarrow n$

Feature, or bug?

- 1. Feature! We create a new unique ID.
- Bug! Bound name has escaped context. Runtime error. (Trigger exception if n evaluated outside scope.)
- 3. Both! Name *n* is an exception, and res is its handler!

fuse is effectful. If fuse n n' is called inside Nom τ monad, it fuses n and n', making them equal. We'll use it for Abs, later.

Equality == on Nom τ follows the monadic structure and is capture-avoiding. Illustrates safe use of unNom.

Let \$ denote right-associative application. For x, y: Nom $\tau \alpha$,

$$x == y \triangleq \text{unNom } x >>= \lambda a.$$

$$y >>= \lambda b.$$

$$\text{return}(a == b).$$

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Recall fresh() \rightarrow res([n], n). Q. Which n?

Equality == on Nom τ follows the monadic structure and is capture-avoiding. Illustrates safe use of unNom.

Let \$ denote right-associative application. For x, y: Nom $\tau \alpha$,

$$x == y \triangleq unNom$$

 $y >>= \lambda b.$
 $y = b.$
 $return(a == b).$

Recall fresh() \rightarrow res([n], n). Which n shouldn't matter; it's abstracted. Then:

$$\begin{aligned} \mathsf{fresh}() &== \mathsf{fresh}() & \to & ???? \\ \mathsf{unNom \$ fresh}() &>> & \lambda a.\mathsf{return}(a == a) & \to & ???? \end{aligned}$$

Equality == on Nom τ follows the monadic structure and is capture-avoiding. Illustrates safe use of unNom.

Let \$ denote right-associative application. For x, y: Nom $\tau \alpha$,

$$x == y \triangleq unNom \ x >>= \lambda a.$$

 $y >>= \lambda b.$
 $return(a == b).$

Recall fresh() \rightarrow res([n], n) for suitable n. Then:

$$fresh() == fresh() \rightarrow False$$

unNom \$ fresh() >>= $\lambda a.return(a == a) \rightarrow ????$

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Equality == on Nom τ follows the monadic structure and is capture-avoiding. Illustrates safe use of unNom.

Let \$ denote right-associative application. For x, y: Nom $\tau \alpha$,

$$x == y \triangleq unNom \ x >>= \lambda a.$$

 $y >>= \lambda b.$
 $return(a == b).$

Recall fresh() \rightarrow res([n], n) for suitable n. Then:

 $\begin{aligned} & \text{fresh}() == \text{fresh}() & \rightarrow & \text{False} \\ & \text{unNom $$ fresh}() >>= \lambda a. \text{return}(a == a) & \rightarrow & \text{True} \end{aligned}$

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Abstraction

Abs : $* \to * \to *$ $\langle - \rangle - :$ $\tau \to \alpha \to \operatorname{Nom} \tau (\tau \times \alpha)$ $\langle n \rangle a \triangleq$ $\operatorname{res}([n], (n, a))$ @@: $\operatorname{Nom} \tau \alpha \to (\tau \times \alpha \to \beta) \to \beta$ $x @@f \triangleq$ $\operatorname{unNom} \$ x >>= \operatorname{return} \circ f$ $\langle n \rangle a @@ f = f(n, a)$ \leftarrow more readable

In words, (n)a is '(n, a) in an n-binding'. Call this abstraction.
 @@ is concretion. It unpacks an abstraction and applies f:

$$\langle n \rangle a @@ f \rightarrow f(n,a).$$

n can escape scope, e.g.

 $\langle n \rangle n @@ \lambda n, a.a \rightarrow n.$ (ロト・(圏ト・(ミト・(ミト ミ のへぐ 20/30))

A simple program

$$\langle n \rangle n @@ \lambda n, a. \langle n \rangle (\langle n \rangle a, a) \rightarrow ????$$

Let's mark the bindings:

$$\langle n^1 \rangle n^1$$
 @@ $\lambda n, a. \langle n^1 \rangle (\langle n^2 \rangle a^2, a^1)$

So:

 $\langle n \rangle n @@ \lambda n, a. \langle n \rangle (\langle n \rangle a, a) \rightarrow \langle n^1 \rangle (\langle n^2 \rangle n^2, n^1)$

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Abs equality

Abs τ - equality is *not* monadic! For x, y : Abs τ :

$$x == x' \triangleq \text{unNom } x >>= \lambda n, a.$$

$$x' >>= \lambda n', a'.$$

$$fuse(n, n') >>$$

$$return(a == a')$$

Above, >>t is >>= $\lambda a.t$ where a is not free in t. So in particular,

$$\langle n \rangle a == \langle n \rangle a \rightarrow \text{True}$$

 $\langle n \rangle a == \langle n' \rangle a' \rightarrow \text{True}$

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A useful test program

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Should this compute True or False?

A useful test program

This should compute False.

Equality is **capture-avoiding** and restriction captures **dynamically**. Each of the two restrictions res([n], n) 'owns' its own local copy of n.

Abs-by-name vs. abs-by-function

-- fresh f returns the value of f at a fresh name atFresh :: t -> (Name t -> a) -> Nom t a atFresh t f = f < fresh t -- Abstract a name in an element absByName :: Name t -> a -> Abs t a absByName n a = Abs \$ res [n] (n, a) -- Apply f to a fresh element of type t absFresh :: t -> (Name t -> a) -> Abs t a absFresh t f = Abs. atFresh t $\ \ m \rightarrow (m, f m)$

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Characteristic property of nominal abstraction

```
-- Concretion of an abstraction at a name.
     Unsafe if name is not fresh.
conc :: Abs m a -> Name m -> a
conc a' m' = a' @@ \m a -> unsafeUnNom $
             fuseLeft [(m, m')]
          >> return a
-- near inverse to <*>;
-- absFuncIn . absFuncOut = id but
-- not necessarily other way around
absFuncOut :: Default t =>
              (Abs t a -> Abs t b) ->
               Abs t (a -> b)
absFuncOut f = absFresh def
   (\n a -> conc (f (absByName n a)) n)
```

This suggests our constructs are relatively powerful.

Let's look at some code

Nominal_IOref.hs SystemF.hs Nominal_resumable_exceptions.hs

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Mathematically, a name n is a datum that is:

- dynamically bindable,
- testable for equality, and
- can be generated fresh.

But this doesn't directly help write a Nominal package for Haskell, Scala, Perl, OCaml, and so forth.

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What's a name?

I propose that a name *n* is a **resumable exception**.

A name is a widget that just holds a **private ID**. It remains passive until triggered with one of two questions:

- A. What is your public ID?
 E.g. == : Name τ → Name τ → Bool tests for equality of public IDs.
- ▶ B. What is your label? label : Name τ → τ queries this.

On query, a name raises an exception labelled with its private ID, which is caught by the innermost handler holding the name's private ID - if this exists!

I recommend not insisting that a handler always exists, so that names are data, not data-in-a-monadic-context.

 I propose that a name n is a **UNIX channel** (e.g. stdio).

A name is a widget that just holds the **private ID** of the channel. It remains passive until triggered with one of two questions:

- A. What is your public ID? E.g. == tests for equality of public IDs.
- B. What is your label? label queries this.

In both cases it queries a channel handler on the private ID.

The handler calculates and answer and returns an answer.

Like cat "Hello world" > filename.txt.